

# Math 162: Calculus IIA

Second Midterm Exam

November 15, 2007

NAME (please print legibly): \_\_\_\_\_

Your University ID Number: \_\_\_\_\_

Indicate your instructor with a check in the box:

Juan Ortiz-Navarro	MWF 9:00 - 9:50 AM	<input type="checkbox"/>
Doug Ravenel	MWF 10:00 - 10:50 AM	<input type="checkbox"/>

- The presence of calculators, cell phones, iPods and other electronic devices at this exam is strictly forbidden.
- Show your work and justify your answers. You may not receive full credit for a correct answer if insufficient work is shown or insufficient justification is given.
- You are responsible for checking that this exam has all 8 pages.

QUESTION	VALUE	SCORE
1	15	
2	15	
3	15	
4	15	
5	15	
6	15	
7	15	
TOTAL	105	

1. (15 points) Find the sum of the series:

$$\sum_{n=0}^{\infty} \frac{2}{3^n}$$

ANSWER: \_\_\_\_\_

2. (15 points) Find the sum of the following series.

$$\sum_{n=1}^{\infty} \frac{3}{n^2 + 2n}$$

**Hint:** Use partial fractions.

ANSWER: \_\_\_\_\_

**3. (15 points)**

Does the following series converge or diverge? Why?

$$\sum_{n=1}^{\infty} \frac{2n}{\ln(n+1)}$$

Justify your answer, making sure to name any convergence or divergence tests that you are using.

ANSWER: \_\_\_\_\_

**4. (15 points)**

Does the following series converge conditionally, converge absolutely or diverge? Why?

$$\sum_{n=1}^{\infty} \frac{(-1)^n}{n \ln n}$$

Justify your answer, making sure to name any convergence or divergence tests that you are using.

ANSWER: \_\_\_\_\_

5. (15 points) Find the radius and interval of convergence of the following power series:

$$\sum_{n=0}^{\infty} (-1)^n \frac{x^{2n}}{(2n)!}$$

ANSWER: \_\_\_\_\_

**6. (15 points)**

Does this series converge or diverge?

$$\sum_{n=1}^{\infty} \frac{2^n(n+1)}{n!}$$

Justify your answer, making sure to name any convergence or divergence tests that you are using.

ANSWER: \_\_\_\_\_

**7. (15 points)**

Find the limit of this sequence.

$$\lim_{n \rightarrow \infty} \frac{2n^2 + 1}{\sqrt{3n^4 + 1}}$$

ANSWER: \_\_\_\_\_